

Structural calculation for Stair 1

Gravity loads:

Stairs, Including landings

2" concrete =	25 psf
Tread/ Riser thickness= 0.081" (12GA) =	4 psf
Misc weight =	6 psf
Total DL =	35 psf
Live load =	100 psf

Design criteria for stair : Design loads are 100 psf uniform load + material DL of stair or a concentrated load of 300 lbs on an area of 4 in² , whichever produce greatest stress.

Hand rail loads: LL = 50 plf or 200 lbs concentrate load act in any direction

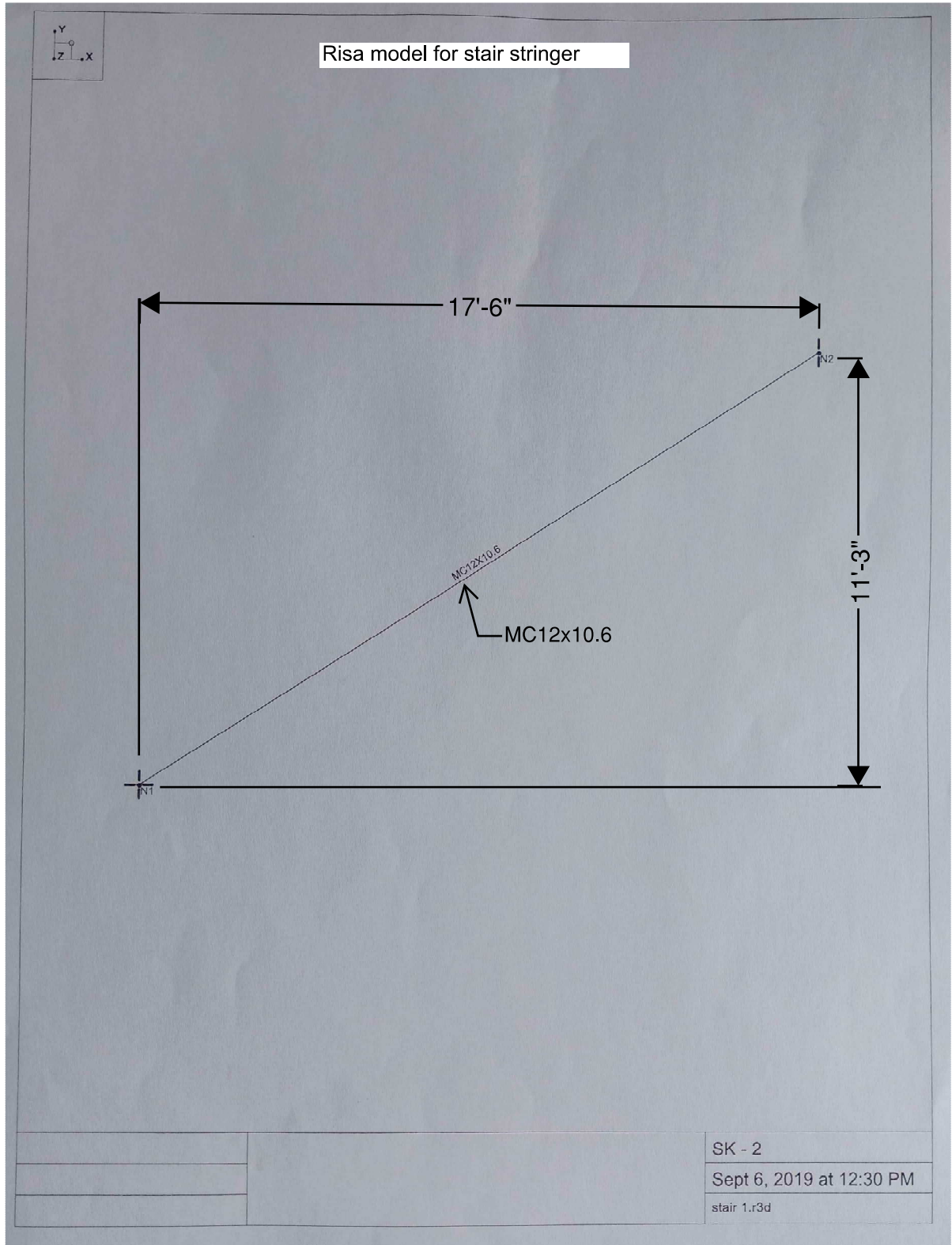
Deflection criteria for DL+LL = L/240 .

Materials

Channels:	ASTM A36, Fy = 36 ksi, Fu = 58 ksi
Pipes:	ASTM A53, Fy = 35 ksi, Fu = 60 ksi
Angles, Plates:	ASTM A36, Fy = 36 ksi, Fu = 58 ksi

Wood: (Assume) Southern pine wood , No.2 grad

Stair Stringer design calc in Risa



Typical Stair Risers

Riser thickness: $t_{\text{riser}} = 0.081''$

Riser depth: $b_{\text{riser}} = 6''$

Riser span: $L_{\text{riser}} = 45''$

Tread run: $L_{\text{tre}} = 11''$

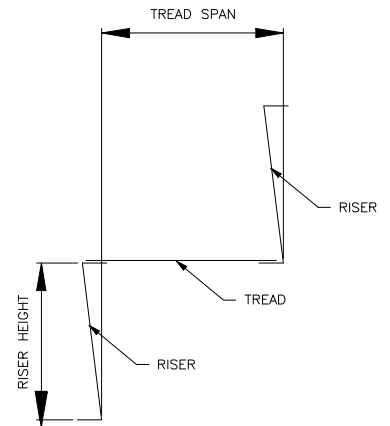
Riser moment of inertia: $I_x = 6^3 \times 0.081 / 12 = 1.458 \text{ in}^4$

Riser plastic modulus: $Z_x = 6^2 \times 0.081 / 4 = 0.729 \text{ in}^4$

Max moment on riser: $M_x = (DL+LL) \times L_{\text{tre}} \times L_{\text{riser}}^2 / 8 = 2611 \text{ lb in}$

Max flexural stress: $f_{b_{\text{Riser}}} = M_x / Z = 3.6 \text{ ksi}$

Allowable flexural stress: $F_b = F_y / 1.67 = 36 / 1.67 = 21.55 \text{ ksi} > f_{b_{\text{Riser}}} \dots \text{OK}$



Check Riser for 300 lb concentrated load

$P_{\text{max}} = 300 \text{ lbs}$

$a_{\text{dist}} = b_{\text{riser}} = 6''$

$b_{\text{dist}} = 2''$ (assume)

$a_{\text{dist}} / b_{\text{dist}} = 3$

From Roark's formulas for stress and strain sixth edition table 35 case 1.1a (rectangular plate under equal uniform compression on two opposite edges, all edges simply supported)

$K_{\text{plate}} = 3.29$, Poisons ratio = 0.32,

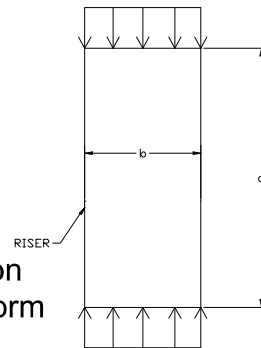
Modulus of elasticity = 29000 ksi

Buckling stress = $3.29 \times 29000 \times (0.081/2)^2 / (1-0.32^2) = 174.34 \text{ ksi} > \text{Yield stress}$, use Yield stress

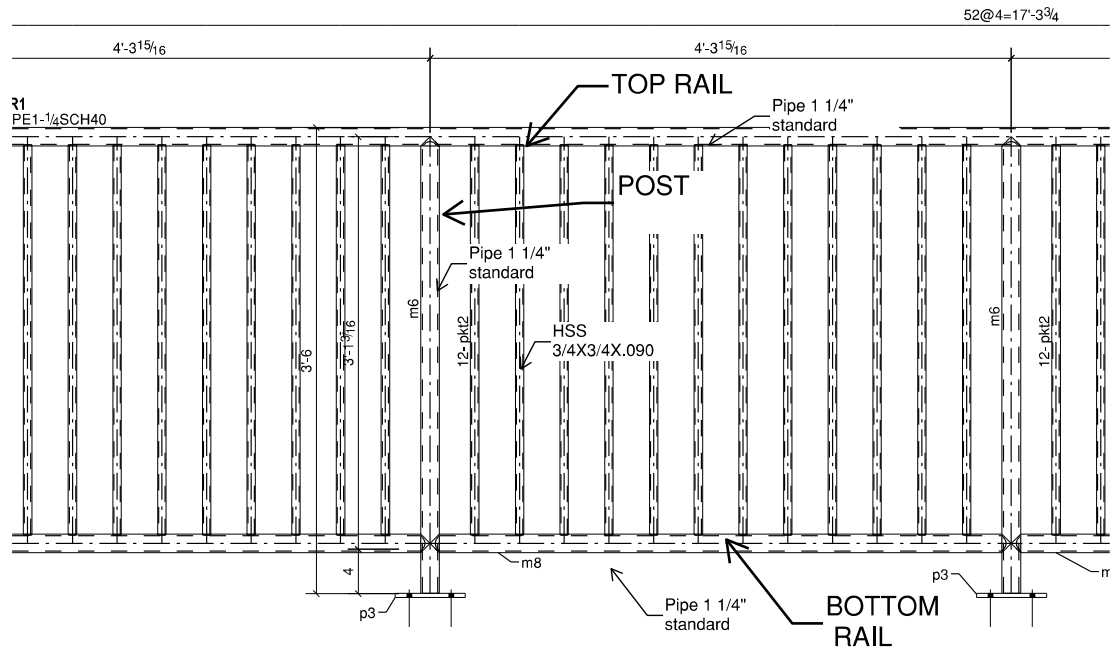
$P_{\text{allow}} = 0.6 F_y b_{\text{dis}} t_{\text{riser}} = 3499 \text{ lbs} > 300 \text{ lbs}.. \text{OK}$

Riser deflection:

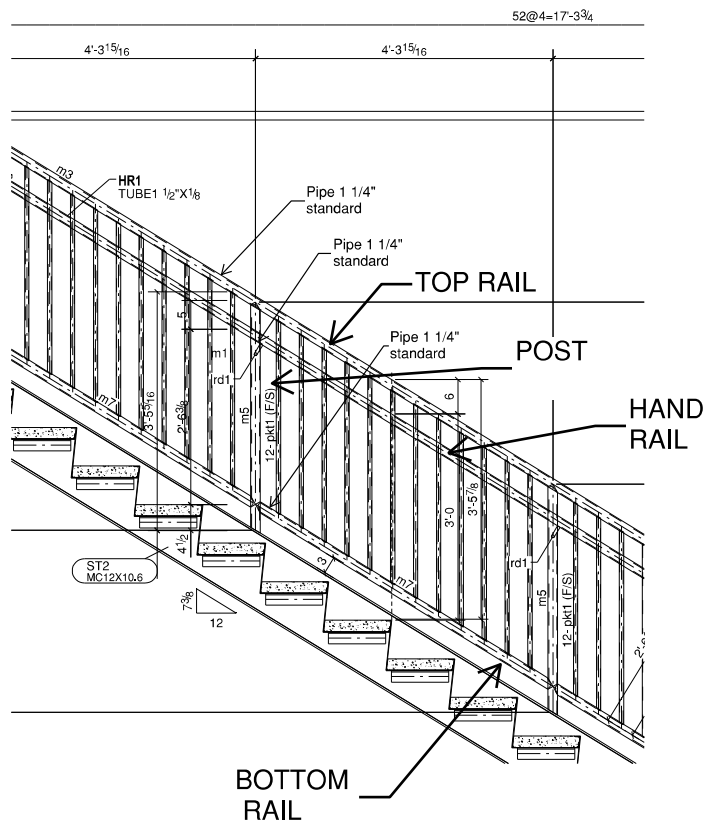
Riser deflection = $300 \times L_{\text{riser}}^3 / (48 \times 29000 \times I_{x_{\text{riser}}}) = 0.013 \text{ in} < L/240 = 0.19 \text{ in}$



Guard rail and Hand rail members design



Guard rail members



Hand rail members

As Hand rail and Guard rail members are same, Hand rail members are govern design and they have longer length

Guard rail and Hand rail members design

Top Rail design:

Top rail length = $L_{\text{rail}} = \text{sqrt}(4.33^2 + 5.67^2) = 5.06 \text{ ft}$

Design loads are

Self weight of member 1 1/4"Ø standard pipe = 2.27 lb/ft

Distributed load, $W = 50 \text{ plf}$ or Point load = 200 lbs (act in any direction)

Max $P_a = 200 \text{ lb}$

Max $V_a = 2.27 \times 5.06/2 + 200 = 206 \text{ lbs}$

Max $M_a = 2.27 \times 5.06^2/8 + 200 \times 5.06/4 = 262 \text{ lb ft.}$

Section Property of 1 1/4"Ø A53 standard pipe

$F_y = 35 \text{ ksi}$

$F_u = 60 \text{ ksi}$

Area = 0.62 in²

$Z = 0.305 \text{ in}^3$

$r = 0.543 \text{ in}$

Compression capacity calc

$KL_{\text{rail}}/r = 112$

Critical stress F_{cr} / factor of safety = 11 ksi (Refer attached page)

Allowable compression capacity = 11 ksi x 0.62 = 6.82 kips > P_a ...**OK**

Shear capacity calc

Shear capacity = $0.6 \times F_y \times A_g / (2 \times 1.67) = 0.6 \times 35 \times 0.62 / (2 \times 1.67) = 3.89 \text{ kips} > V_a$...**OK**

Moment capacity calc

Bending stress = $M_a / Z = 262 \text{ lb/ft} \times 12 / (0.305 \text{ in}^3 \times 1000) = 10.3 \text{ ksi}$

allowable stress = $F_y / 1.67 = 20.95 \text{ ksi} > 10.3 \text{ ksi}$**OK**

Top Stringer floor connection with wood

Load = 3 kips (refer Risa results)

Assume wood Southern pine wood , No.2 grad

Members are (3) 2x12 member,

use 3/4"Ø through bolts for connection.

Use NDS 2015

table 11.3.1,

$Z' = Z \times C_D \times C_m \times C_t \times C_g \times C_{\Delta} \times C_{eg} \times C_{di} \times C_{tn}$

$C_{eg} = C_{di} = C_{tn} = 1.0$ (as this is not applicable)

$z = (760+1000)/2 = 880$ lbs (table 12B, NDS) (refer next page)

$C_D = 1.0$ (occupancy live load , table 2.3.2, NDS)

$C_m = 1.0$ (Table 11.3.3, NDS)

$C_t = 1.0$ (Table 11.3.4, NDS)

$C_g = 1.0$ (Table 11.3.6C, NDS), $A_m/A_s = 4 \times 1.5 / 0.25 = 24$

$C_{\Delta} = 1.0$ (edge distance and spacing is min $4D = 4 \times 3/4 = 3$ "

$Z' = 880$ lbs

total require capacity = $3 \text{ kips} / 0.88 \text{ k} = 3.4$ nos 3/4"Ø through bolts works, Provide 4 nos total

